### Overview "Unions and unemployment benefits"

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### Introduction

- one capitalist (player 1) who may employ
- 1 or 2 workers (players 2 and 3)

Two partitions:

• AD-partition:

$$\mathcal{P}_{AD} = \{\{1,2,3\}\}$$
 or  $\mathcal{P}_{AD} = \{\{1,2\},\{3\}\}$ 

• Union partition:

$$\mathcal{P}_u = \{\{1\}$$
 ,  $\{2\}$  ,  $\{3\}\}$  or  $\mathcal{P}_u = \{\{1\}$  ,  $\{2,3\}\}$ 

# The union outside-option value AD-value

#### Lemma (A rank-order definition of the AD-value)

The AD-value is given by

$$AD_{i}\left(\mathbf{v},\mathcal{P}
ight)=rac{1}{n!}\sum_{
ho\in RO}MC_{i}^{K_{i}\left(
ho
ight)\cap\mathcal{P}\left(i
ight)}\left(\mathbf{v}
ight)$$
 ,  $i\in N$ 

According to this alternative characterization of the AD-value, we consider all rank orders but disregard all players outside player *i*'s component.

### The union outside-option value

Generalized Wiese value

#### Definition (generalized Wiese value)

The generalized Wiese value is the solution function W given by

$$W_{i}(v, \mathcal{P}_{AD}, \lambda) = \frac{1}{n!} \sum_{\rho \in RO} \begin{cases} v\left(\mathcal{P}_{AD}(i)\right) - \sum_{j \in \mathcal{P}_{AD}(i) \setminus \{i\}} MC_{j}, & \mathcal{P}_{AD}(i) \subseteq K_{i}(\rho), \\ MC_{i}, & \text{otherwise,} \end{cases}$$

 $\lambda \in [0,1]$  and

$$\mathcal{MC}_{i} := \mathcal{MC}_{i}\left(
ho, \mathcal{P}_{AD}, \lambda
ight) = \lambda \mathcal{MC}_{i}^{\mathcal{K}_{i}\left(
ho
ight)}\left(\mathbf{v}
ight) + \left(1-\lambda
ight) \mathcal{MC}_{i}^{\mathcal{K}_{i}\left(
ho
ight) \cap \mathcal{P}_{AD}\left(i
ight)}\left(\mathbf{v}
ight).$$

 $\lambda = 1 \longrightarrow$  Wiese value  $\lambda = 0 \longrightarrow$  AD-value (component efficiency!)  $\lambda > 0 \longrightarrow$  outside options important

### Definition (union outside-option value)

The union outside-option value is the solution function OW given by

$$\begin{array}{l} & OW_{i}\left(v,\mathcal{P}_{AD},\lambda,\mathcal{P}_{u}\right) \\ = & \frac{1}{\left|RO_{\mathcal{P}_{u}}\right|}\sum_{\rho\in RO_{\mathcal{P}_{u}}} \left\{ \begin{array}{c} v\left(\mathcal{P}_{AD}\left(i\right)\right) - \sum_{j\in\mathcal{P}\left(i\right)\setminus i}MC_{j}, & \mathcal{P}_{AD}\left(i\right)\subseteq K_{i}\left(\rho\right), \\ MC_{i}, & \text{otherwise,} \end{array} \right. \end{array}$$

 $\lambda \in [\mathsf{0},\mathsf{1}]$  and

$$MC_{i} := MC_{i}(\rho, \mathcal{P}_{AD}, \lambda) = \lambda MC_{i}^{K_{i}(\rho)}(v) + (1-\lambda) MC_{i}^{K_{i}(\rho) \cap P_{AD}(i)}(v).$$

partitions and payoffs I

zero normal profits for the capitalist:  $v(\{1\}) := 0$ specification: v(N) := 100,  $a_2 := v(\{1,2\})$ ,  $a_3 := v(\{1,3\})$  with  $a_2 > a_3 \ge 0$ . unemployment benefits:  $v(\{2\}) = v(\{3\}) = u$  and  $v(\{2,3\}) = 2u$ 

$$\begin{array}{cccc} \mathcal{P}_{AD} & \mathcal{P}_{u} & OW\left(v, \mathcal{P}_{AD}, \lambda, \mathcal{P}_{u}\right) \\ \left\{\left\{1, 2, 3\right\}\right\} & \left\{\left\{1\right\}, \left\{2\right\}, \left\{3\right\}\right\} & \begin{pmatrix} A := \frac{100}{3} + \frac{a_{2}}{6} + \frac{a_{3}}{6} - u \\ B := \frac{100}{3} + \frac{a_{2}}{6} - \frac{a_{3}}{3} + \frac{u}{2} \\ C := \frac{100}{3} - \frac{a_{2}}{3} + \frac{a_{3}}{6} + \frac{u}{2} \end{pmatrix} \\ \left\{\left\{1, 2, 3\right\}\right\} & \left\{\left\{1\right\}, \left\{2, 3\right\}\right\} & \begin{pmatrix} D := 50 - u \\ E := 25 + \frac{a_{2}}{4} - \frac{a_{3}}{4} + \frac{u}{2} \\ F := 25 - \frac{a_{2}}{4} + \frac{a_{3}}{4} + \frac{u}{2} \end{pmatrix} \end{array}$$

partitions and payoffs II

$$\begin{array}{ll} \mathcal{P}_{AD} & \mathcal{P}_{u} & OW\left(v, \mathcal{P}_{AD}, \lambda, \mathcal{P}_{u}\right) \\ \left\{\left\{1, 2\right\}, \left\{3\right\}\right\} & \left\{\left\{1\right\}, \left\{2\right\}, \left\{3\right\}\right\} & \begin{pmatrix} G := \frac{a_{2}}{2} + \frac{1}{6}\lambda\left(a_{3} - u\right) - \frac{u}{2} \\ H := \frac{a_{2}}{2} - \frac{1}{6}\lambda a_{3} + \frac{1}{6}u\left(3 + \lambda\right) \\ = \frac{a_{2}}{2} - \frac{1}{6}\lambda\left(a_{3} - u\right) + \frac{u}{2} \\ I := u \\ I := u \\ \end{pmatrix} \\ \left\{\left\{1, 2\right\}, \left\{3\right\}\right\} & \left\{\left\{1\right\}, \left\{2, 3\right\}\right\} & \begin{pmatrix} J := \frac{a_{2}}{2} - \frac{u}{2} \\ K := \frac{a_{2}}{2} + \frac{u}{2} \\ L := u \end{pmatrix} \\ \left\{\left\{1\right\}, \left\{2\right\}, \left\{3\right\}\right\} & \left\{\left\{1\right\}, \left\{2\right\}, \left\{3\right\}\right\} & \begin{pmatrix} M := 0 \\ N := u \\ P := u \end{pmatrix} \\ \end{array} \right\} \end{array}$$

partitions and payoffs III

- The capitalist prefers to have worker 2 rather than worker 3 as his only employee (profits G and J).
- Unemployment benefits increase wages.
- If worker 2 is the only employee and if the workers are not unionized, worker 2's payoff

$$H = \frac{a_2}{2} - \frac{1}{6}\lambda\left(a_3 - u\right) + \frac{1}{2}u$$

reveals that the capitalist can use worker 3 to lower worker 2's wage. This mechanism will work,

- if there is a high degree of flexibility and outside options ( $\lambda$  is high),
- if worker 3 is productive (if he were employed), and
- if unemployment benefits are moderate.

Karl Marx' industrial reserve ....

### A simple labour market partitions and payoffs IV

- Union: capitalist employs worker 3, too, if  $100 a_2 > u$ .
- No union: By

$$A > G \Leftrightarrow 100 - a_2 > \frac{1}{2} \left[ u \left( 3 - \lambda \right) - a_3 \left( 1 - \lambda \right) \right]$$

capitalist might employ worker 3 even if  $100 - a_2 < 0$  holds (right hand side may be negative)

- productiveness
- versus bargaining effect
- The two workers prefer a union if
  - average productivity in a one-worker firm is sufficiently high, or differently put,
  - average marginal contribution is sufficiently low  $(\frac{1}{2}(100 a_3) + \frac{1}{2}(100 a_2) < 50) \longrightarrow$  overstaffing

game sequence

- The workers decide on unionization.
- The capitalist makes an employment offer to worker 2, worker 3, both, or none. (Wages are determined later.)
- The workers accept employment or decline:
  - If any worker declines, no workers are employed.
  - Since the capitalist can foresee the workers' payoffs and decisions, he will make acceptable offers.
- Wages and profits are determined. We assume  $\lambda := 1$ .

voluntary unemployment can happen

Definition: An unemployed worker is voluntarily unemployed if employing him - on top of the actually employed workers - would lead to an unattractive wage rate, i.e., a wage rate lower than his unemployment benefit.

Figure: no union,  $a_3 < 50$ ,  $25 + \frac{a_3}{2} < a_2 < \frac{400}{13} + \frac{5a_3}{13}$ 

Capitalist:	2	none both	none		both	2
Worker 2:			yes	no		
Both workers:				yes	no	
Accepted offer:		both	none			
		full employment	involuntary unemployment of both workers	involuntary unemployment of worker 3	voluntary unemployment of both workers	

Uemployment is an increasing function of the level of unemployment benefits. But the effect of unions is unclear; consider the leftmost triangle bordering the *u*-axis and the very small triangle to the right of this triangle:



### A simple labour market union choice (stage 1) - a3=20

Two distinct reasons for unionization:

- obtaining a salary instead of unemployment benefits and/or
- increasing salary



If both workers are employed, their preferences coincide. Therefore, unions can never be blamed for unemployment from the point of view of stage 1.

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Applied cooperative game theory:

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